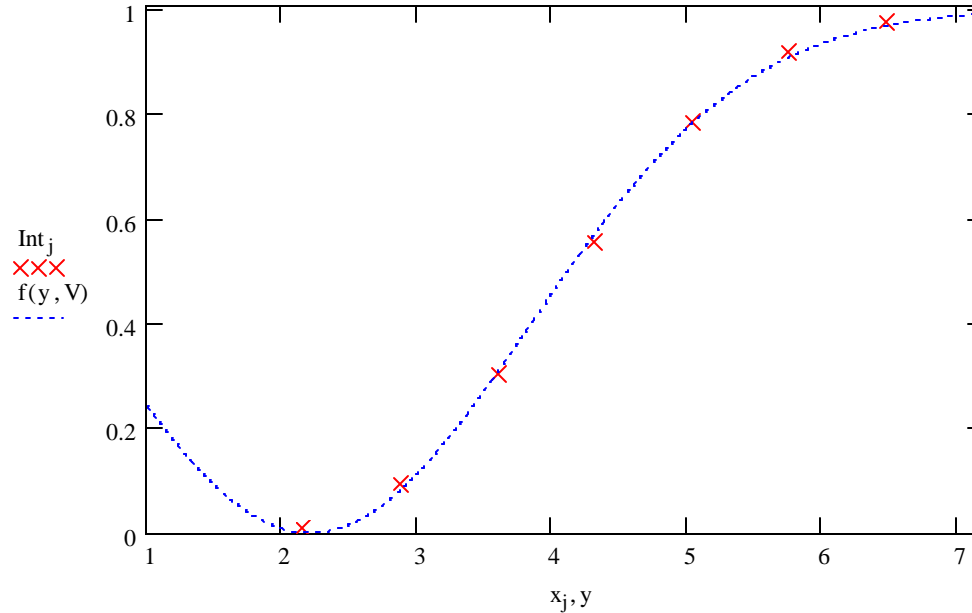


### Study plan

1. Reference measurements
  - Measure beam current as function of scraper position
2. Measurements
  - Inject new beam
  - Scrape to 75% of initial current horizontally and then to 50% vertically
  - Remove scrapers
  - Wait 1 hour
  - Measure beam current as function of scraper position

### Reference Measurement and its fitting



Dependence of beam current (T:IBEAM) on position of the vertical collimator (T:E01VCP);  $\times$  - measurements, dotted line – fitting for gaussian an distribution

## Theoretical description

For Coulomb scattering one can write an equation which simultaneously describe single and multiple scattering

$$\frac{\partial f}{\partial t} = \frac{D}{2L_c} \int_0^\infty \left[ \frac{I' + I}{\left( (I' - I)^2 + (I' + I)\Delta I \right)^{3/2}} - \frac{1}{\Delta I} \mathbf{d}(I' - I) \right] f(I') dI'$$

If one neglects single scattering this equation yields the standard diffusion equation for an oscillator

$$\frac{\partial f}{\partial t} = D \frac{\partial}{\partial I} \left( I \frac{\partial f}{\partial I} \right).$$

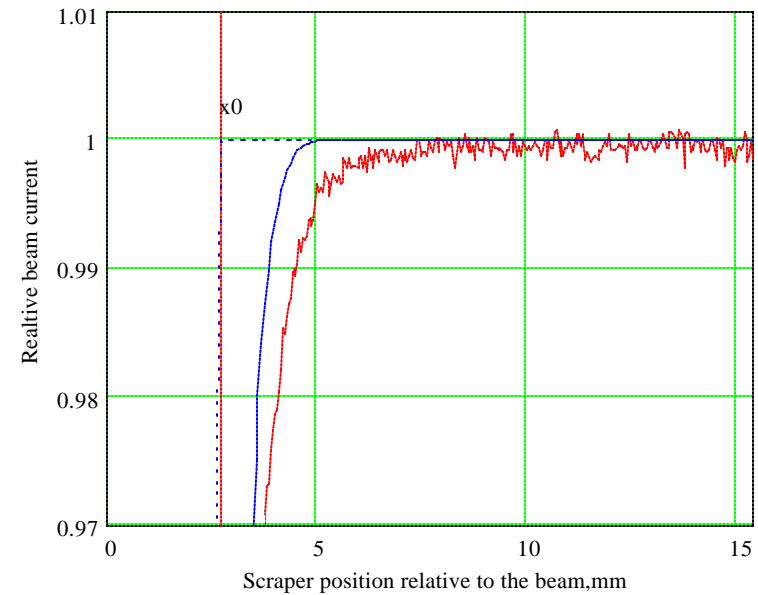
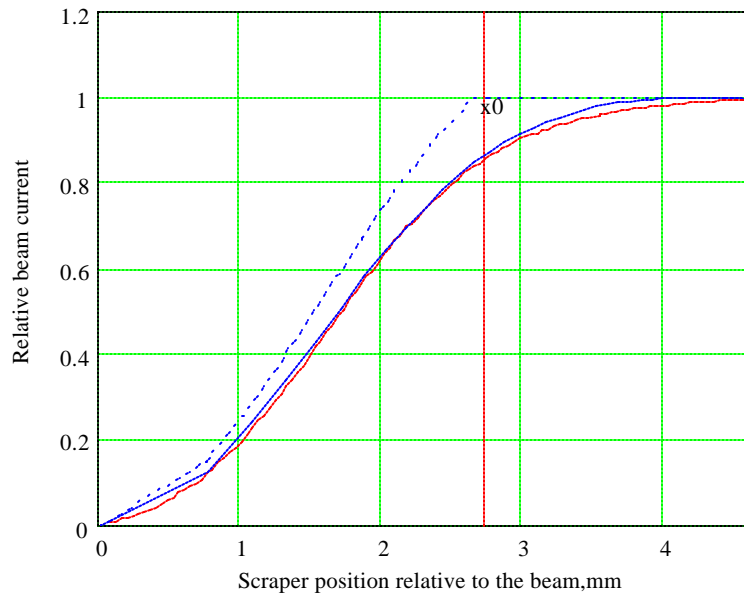
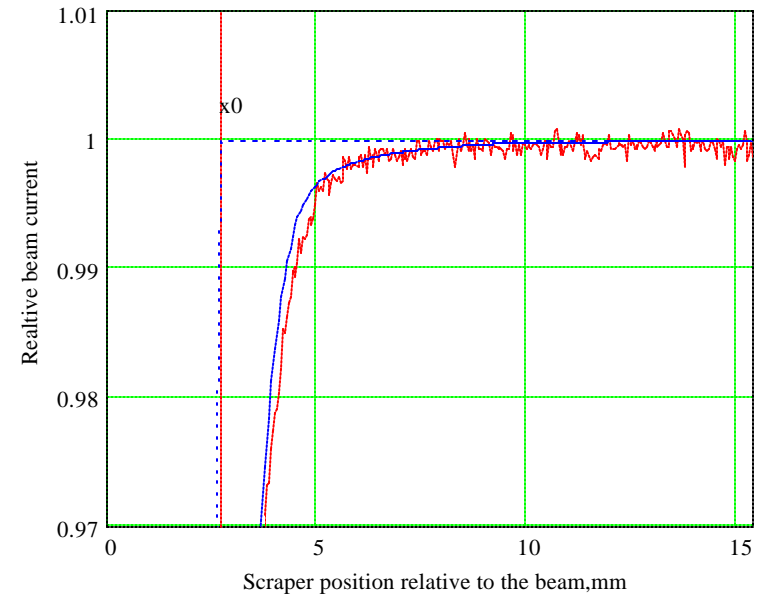
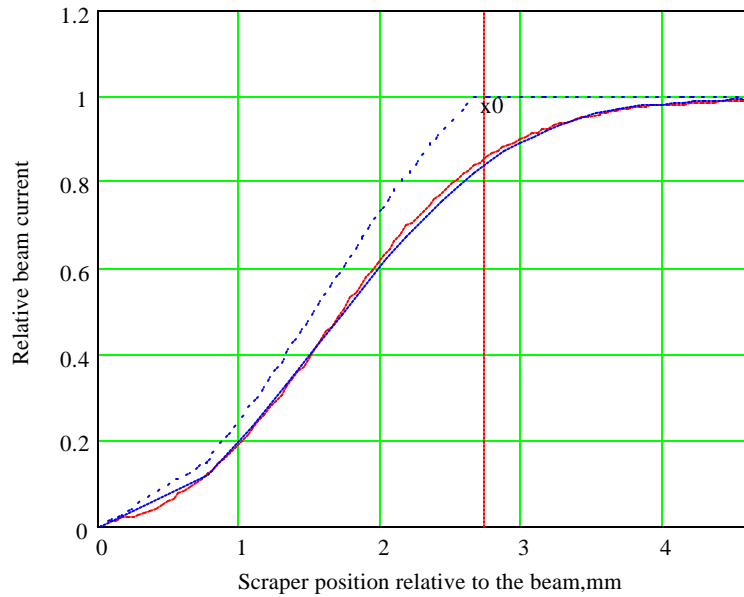
Here  $L_c$  is the Coulomb logarithm,

$$I = \frac{x^2}{\mathbf{b}} (1 + \mathbf{a}^2) + 2\mathbf{a}xx' + \mathbf{b}x'^2 \text{ is the action,}$$

$$D = \frac{4pe^4 L_c}{P^2 v_0} \sum_i Z_i^2 n_i \oint \mathbf{b}(s) \frac{ds}{L} \text{ is the diffusion coefficient,}$$

and  $\mathbf{b}(s)$  is the beta-function.

## Measurement results



Dependence of the beam current on scraper positions after scraping the beam to 12 mm mrad and 1 hour beam expansion. Top - both multiple and single scattering are taken into account in the simulations; bottom - only multiple scattering is taken into account in the simulations. Blue line theory prediction, red -lines measurement results. Right side presents the same data but with better resolution of tails.

## Conclusions

1.

Acceptance of the machine corresponding to initial scraper position	12 mm mrad
Measured emittance growth rate at 150 GeV	4.9 mm mrad / hour
Average vacuum expressed in the atomic hydrogen pressure	$4.1 \cdot 10^{-7}$ Torr

2. If we presume the same gas composition the average vacuum is approximately 20 times worse then in the Accumulator
3. Gas scattering is a major source of the beam heating. Coincidence between measured population in the tails and the model suggest that at least 80% of the transverse beam heating is related to multiple scattering on the residual gas. There may be larger contribution of the gas scattering but statistical accuracy of the data and not-sufficiently gaussian distribution of initial beam limit the coincidence between the theory and the measurements.

$$p_{\max} 10^9 = \begin{pmatrix} 14.42 \\ 18.54 \\ 0.618 \\ 0.309 \\ 0.258 \\ 0.515 \\ 0.309 \\ 0.412 \end{pmatrix} = \begin{pmatrix} \text{H} \\ \text{H}_2 \\ \text{CO} \\ \text{N}_2 \\ \text{C}_2\text{H}_2 \\ \text{C}_2\text{H}_4 \\ \text{CO}_2 \\ \text{Ar} \end{pmatrix}$$